Economics 471: Introductory Econometrics Department of Economics, Finance and Legal Studies University of Alabama Fall 2023

Midterm I

The exam consists of three questions on three pages. Each question is of equal value.

- 1. Suppose we observe a random sample of data $\{x_i, y_i\}_{i=1}^n$. Consider the model $y_i = \alpha + u_i$, where $u_i \sim (0, \sigma^2)$. With this information, answer the following:
 - (a) Derive the ordinary least-squares estimator of α .
 - (b) For the estimator derived in part (a), derive its variance.
 - (c) What happens to the variance of the estimator in part (b) as the sample size (n) increases?
 - (d) What happens to the variance of the estimator in part (b) as the error variance (σ^2) increases?
 - (e) What happens to the variance of the estimator in part (b) when the total variation in x $(\sum_{i=1}^{n} (x_i - \bar{x})^2)$ increases?

- 2. Consider the population regression function $Y = \alpha + \beta X + U$, where $U \sim (0, \sigma^2)$. Assuming $\alpha > 0$ and $\beta < 0$, in the figure below, perform the following:
 - (a) Label the axes
 - (b) Plot and label the population regression line.
 - (c) Pick an arbitrary value for X, say x', and plot its conditional expectation (i.e., E(Y|X = x')).
 - (d) Plot and label the distribution of the error (U) about its conditional expectation for the point you listed in part (c).
 - (e) Suppose there was a one unit increase in the value you picked for X in part (b). What is the marginal impact on the conditional expectation from that one unit increase (x' to x' + 1)? Show this on the figure.

3. Consider the gretl output below for cross-country data on the number of deaths per 100,000 individuals (*deaths*) versus the liters of alcohol consumed from wine, per capita (*alcohol*). With this information, answer the following (give all formulae used):

Model 1: OLS, using observations 1–21 Dependent variable: *deaths*

	Coeffici		ent Std. I		Error	t-ratio	p-val	ue
	const 876.205		5 30.468		82	28.76	0.000	0
	alcohol	-16.263	35	8.198	892	-1.984	0.061	9
Mean	dependent	t var	830.0	0476	S.D. 6	lependent	var	96.51864
Sum squared resid			154352.0		S.E. of regression		n	90.13207
R^2			0.171	1562	Adjus	sted R^2		0.127960
F(1, 19)	9)		3.934	4731	P-val	ue(F)		0.061939
Log-lil	kelihood	_	-123.2	2736	Akaik	e criterion	L	250.5473
Schwar	rz criterio	n	252.6	6363	Hann	an–Quinn		251.0006

- (a) What is the estimated variance of the number of deaths $(\hat{\sigma}_{deaths}^2)$?
- (b) What is the estimated error variance $(\hat{\sigma}^2)$?
- (c) Interpret the intercept coefficient. Does this appear to be reasonable?
- (d) Interpret the slope coefficient. Does this appear to be reasonable?
- (e) What percentage of the variation in deaths can be explained by the variation in alcohol consumption?